

CCGPS 2nd Grade Grade Level Overview

Mathematics

Second Grade Grade Level

Overview



Dr. John D. Barge, State School Superintendent "Making Education Work for All Georgians"

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Common Core Georgia Performance Standards Framework

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Common Core Georgia Performance Standards Second Grade

Common Core Georgia Performance Standards: Curriculum Map								
Unit 1	Unit 2	Unit 3	Unit 4	Unit 5	Unit 6	Unit 7		
Extending Base Ten Understanding	Becoming Fluent with Addition and Subtraction	Understanding Measurement, Length, and Time	Applying Base Ten Understanding	Understanding Plane and Solid Figures	Developing Multiplication	Show What We Know		
MCC2.NBT.1 MCC2.NBT.2 MCC2.NBT.3 MCC2.NBT.4 MCC2.MD.10	MCC2.OA.1 MCC2.OA.2 MCC2.NBT.5 MCC2.MD.8 MCC2.MD.10	MCC2.MD.1 MCC2.MD.2 MCC2.MD.3 MCC2.MD.4 MCC2.MD.5 MCC2.MD.6 MCC2.MD.7 MCC2.MD.7 MCC2.MD.9 MCC2.MD.10	MCC2.NBT.6 MCC2.NBT.7 MCC2.NBT.8 MCC2.NBT.9 MCC2.MD.8 MCC2.MD.10	MCC2.G.1 MCC2.G.2 MCC2.G.3 MCC2.MD.10	MCC2.OA.3 MCC2.OA.4 MCC2.MD.10	ALL		
The	These units were written to build upon concepts from prior units, so later units contain tasks that depend upon the concepts addressed in earlier units.							
All units will include the Mathematical Practices and indicate skills to maintain.								

NOTE: Mathematical standards are interwoven and should be addressed throughout the year in as many different units and tasks as possible in order to stress the natural connections that exist among mathematical topics.

Grades K-2 Key: CC = Counting and Cardinality, G= Geometry, MD=Measurement and Data, NBT= Number and Operations in Base Ten, OA = Operations and Algebraic Thinking.

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STANDARDS FOR MATHEMATICAL PRACTICE

The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. These practices rest on important "processes and proficiencies" with longstanding importance in mathematics education.

The first of these are the NCTM process standards of problem solving, reasoning and proof, communication, representation, and connections.

The second are the strands of mathematical proficiency specified in the National Research Council's report Adding It Up: adaptive reasoning, strategic competence, conceptual understanding (comprehension of mathematical concepts, operations and relations), procedural fluency (skill in carrying out procedures flexibly, accurately, efficiently and appropriately), and productive disposition (habitual inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one's own efficacy).

Students are expected to:

1. Make sense of problems and persevere in solving them.

In second grade, students realize that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. They may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, "Does this make sense?" They make conjectures about the solution and plan out a problem-solving approach.

2. Reason abstractly and quantitatively.

Younger students recognize that a number represents a specific quantity. They connect the quantity to written symbols. Quantitative reasoning entails creating a representation of a problem while attending to the meanings of the quantities. Second graders begin to know and use different properties of operations and objects.

3. Construct viable arguments and critique the reasoning of others.

Second graders may construct arguments using concrete referents, such as objects, pictures, drawings, and actions. They practice their mathematical communication skills as they participate in mathematical discussions involving questions like "How did you get that?", "Explain your thinking," and "Why is that true?" They not only explain their own thinking, but listen to others' explanations. They decide if the explanations make sense and ask appropriate questions.

4. Model with mathematics.

In early grades, students experiment with representing problem situations in multiple ways including numbers, words (mathematical language), drawing pictures, using objects, acting out, making a chart or list, creating equations, etc. Students need opportunities to connect the different representations and explain the connections. They should be able to use all of these representations as needed.

5. Use appropriate tools strategically.

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In second grade, students consider the available tools (including estimation) when solving a mathematical problem and decide when certain tools might be better suited. For instance, second graders may decide to solve a problem by drawing a picture rather than writing an equation.

6. Attend to precision.

As children begin to develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and when they explain their own reasoning.

7. Look for and make use of structure.

Second graders look for patterns. For instance, they adopt mental math strategies based on patterns (making ten, fact families, doubles).

8. Look for and express regularity in repeated reasoning.

Students notice repetitive actions in counting and computation, etc. When children have multiple opportunities to add and subtract, they look for shortcuts, such as rounding up and then adjusting the answer to compensate for the rounding. Students continually check their work by asking themselves, "Does this make sense?"

Mathematical Practices 1 and 6 should be evident in EVERY lesson

CONTENT STANDARDS

OPERATIONS AND ALGEBRAIC THINKING (OA)

CLUSTER #1: REPRESENT AND SOLVE PROBLEMS INVOLVING ADDITION AND SUBTRACTION.

MCC2.OA.1 Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

This standard calls for students to add and subtract numbers within 100 in the context of one and two step word problems. Students should have ample experiences working on various types of problems that have unknowns in all positions, including:

Addition Examples:

Result Unknown	Change Unknown	Start Unknown
There are 29 students on the	There are 29 students on the	There are some students on
playground. Then 18 more	playground. Some more	the playground. Then 18
students showed up. How	students show up. There are	more students came. There
many students are there	now 47 students. How many	are now 47 students. How
now?	students came? (29 + =	many students were on the
(29 + 18 =)	47)	playground at the beginning?
,		(+ 18 = 47)

See Table 1 at the end of this document for more addition examples as well as subtraction examples.

This standard also calls for students to solve one- and two-step problems using drawings, objects and equations. Students can use place value blocks or hundreds charts, or create drawings of place value blocks or number lines to support their work. Examples of one-step problems with unknowns in different places are provided in Table 1. Two step-problems include situations where students have to add and subtract within the same problem.

Example:

In the morning there are 25 students in the cafeteria. 18 more students come in. After a few minutes, some students leave. If there are 14 students still in the cafeteria, how many students left the cafeteria? Write an equation for your problem.

Student 1

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Step 1	I used place value blocks and made a group of 25 and a group of 18. When I counted them I had 3 tens and 13 ones which is 43.	
Step 2	I then wanted to remove blocks until there were only 14 left. I removed blocks until there were 20 left.	
Step 3	Since I have two tens I need to trade a ten for 10 ones.	
Step 4	After I traded it, I removed blocks until there were only 14 remaining.	
Step 5	My answer was the number of blocks that I re That's 29.	emoved. I removed 2 tens and 9 ones.
	My equation is $25 + 18 - _ = 14$.	

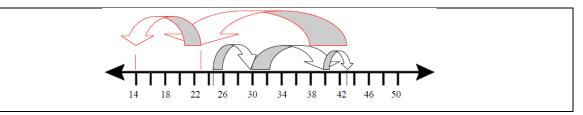
Student 2

I used a number line. I started at 25 and needed to move up 18 spots so I started by moving up 5 spots to 30, and then 10 spots to 40, and then 3 more spots to 43. Then I had to move backwards until I got to 14 so I started by first moving back 20 spots until I got to 23. Then I moved to 14 which were an additional 9 places. I moved back a total of 29 spots. Therefore there were a total of 29 students left in the cafeteria. My equation is $25 + 18 - \underline{} = 14$.

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Student 3

Step	I used a hundreds board. I started at	1	2	3	4	5	6	7	8	9	10
1	25. I moved down one row which is	11	12	13	14	15	16	17	18	19	20
	10 more, then moved to the right 8	21	22	23	24	25	26	27	28	29	30
	spots and landed on 43. This	31	32	33	34	35	36	37	38	39	40
	represented the 18 more students	4 <u>1</u>	42	43	44	45	46	47	48	49	50
	coming into the cafeteria.	51	52	53	54	55	56	57	58	59	60
	coming into the careteria.	61	62	63	64	65	66	67	68	69	70
		71	72	73	74	75	76	77	78	79	80
		81	82	83	84	85	86	87	88	89	90
		91	92	93	94	95	96	97	98	99	100
Step	Now starting at 43, I know I have to	1	2	3	4	5	6	7	8	9	10
2	get to the number 14 which	11	12	13	14	15	16	17	18	19	20
	represents the number of students	21	22	23	24	25	26	27	28	29	30
	left in the cafeteria so I moved up 2	31	32	33	34	35	36	37	38	39	40
	rows to 23 which is 20 less. Then I	41	42	(43)	44	45	46	47	48	49	50
		51	52	53	54	55	56	57	58	59	60
	moved to the left until I land on 14,	61	62	63	64	65	66	67	68	69	70
	which is 9 spaces. I moved back a	71	72	73	74	75	76	77	78	79	80
	total of 29 spots. That means 29	81	82	83	84	85	86	87	88	89	90
	students left the cafeteria.	91	92	93	94	95	96	97	<u>98</u>	99	100
Step 3	My equation to represent this situation	n is 25	+ 18	8 – _	=	: 14.					

CLUSTER #2: ADD AND SUBTRACT WITHIN 20.

MCC2.OA.2 Fluently add and subtract within 20 using mental strategies.2 By end of Grade 2, know from memory all sums of two one-digit numbers.

This standard mentions the word *fluently* when students are adding and subtracting numbers within 20. Fluency means accuracy (correct answer), efficiency (within 4-5 seconds), and flexibility (using strategies such as making 10 or breaking apart numbers). Research indicates that teachers' can best

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support students' memorization of sums and differences through varied experiences making 10, breaking numbers apart and working on mental strategies, rather than repetitive timed tests.

Example: 9 + 5 =____

Student 1: Counting On

I started at 9 and then counted 5 more. I landed at 14.

Student 2: *Decomposing a Number Leading to a Ten*

I know that 9 and 1 is 10, so I broke 5 into 1 and 4. 9 plus 1 is 10. Then I have to add 4 more, which gets me to 14.

Example: 13 – 9 = ____

Student 1: Using the Relationship between Addition and Subtraction

I know that 9 plus 4 equals 13. So 13 minus 9 equals 4.

Student 2: Creating an Easier Problem

I added 1 to each of the numbers to make the problem 14 minus 10. I know the answer is 4. So 13 minus 9 is also 4.

CLUSTER #3: WORK WITH EQUAL GROUPS OF OBJECTS TO GAIN FOUNDATIONS FOR MULTIPLICATION.

<u>MCC2.OA.3 Determine whether a group of objects (up to 20) has an odd or even number of</u> members, e.g., by pairing objects or counting them by 2s; write an equation to express an even number as a sum of two equal addends.

This standard calls for students to apply their work with doubles addition facts to the concept of odd or even numbers. Students should have ample experiences exploring the concept that if a number can be decomposed (broken apart) into two equal addends (e.g., 10 = 5 + 5), then that number (10 in this case) is an even number. Students should explore this concept with concrete objects (e.g., counters, place value cubes, etc.) before moving towards pictorial representations such as circles or arrays.

Example: Is 8 an even number? Prove your answer.

Student 1

I grabbed 8 counters. I paired counters up into groups of 2. Since I didn't have any counters left over, I know that 8 is an even number.

Student 2

I grabbed 8 counters. I put them into 2 equal groups. There were 4 counters in each group, so 8 is an even number.

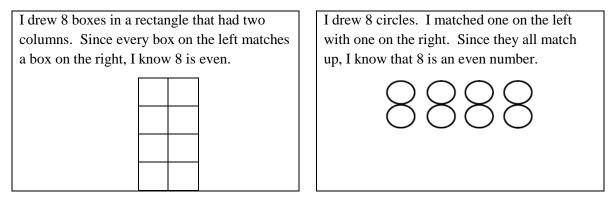
Student 3

Student 4

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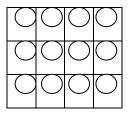
Student 5

I know that 4 plus 4 equals 8. So 8 is an even number.

Find the total number of objects below.

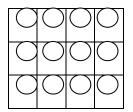
Student 1

I see 3 counters in each column and there are 4 columns. So I added: 3 + 3 + 3 + 3. That equals 12.



Student 2

I see 4 counters in each row and there are 3 rows. So I added 4 + 4 + 4. That equals 12.



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NUMBER AND OPERATIONS IN BASE TEN (NBT)

CLUSTER #1: UNDERSTAND PLACE VALUE.

Students extend their understanding of the base-ten system. This includes ideas of counting in fives, tens, and multiples of hundreds, tens, and ones, as well as number relationships involving these units, including comparing. Students understand multi-digit numbers (up to 1000) written in base-ten notation, recognizing that the digits in each place represent amounts of thousands, hundreds, tens, or ones (e.g., 853 is 8 hundreds + 5 tens + 3 ones).

<u>MCC2.NBT.1 Understand that the three digits of a three-digit number represent amounts of</u> <u>hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following</u> <u>as special cases:</u>

This standard calls for students to work on decomposing numbers by place. Students should have ample experiences with concrete materials and pictorial representations examining that numbers all numbers between 100 and 999 can be decomposed into hundreds, tens, and ones.

Interpret the value of a digit (1-9 and 0) in a multi-digit numeral by its position within the number with models, words and numerals.

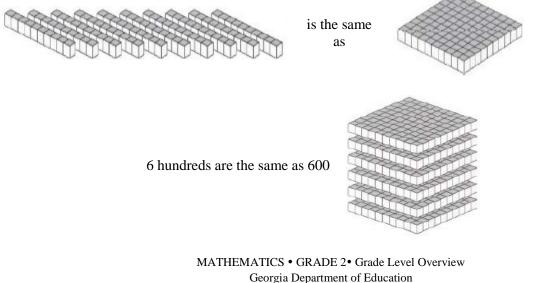
Use 10 as a benchmark number to compose and decompose when adding and subtracting whole numbers.

a. 100 can be thought of as a bundle of ten tens — called a "hundred."

MCC2.NBT.1a calls for students to extend their work from 1st Grade by exploring a hundred as a unit (or bundle) of ten tens.

b. The numbers 100, 200, 300, 400, 500, 600, 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).

MCC2.NBT.1b builds on the work of MCC2.NBT.1a. Students should explore the idea that numbers such as 100, 200, 300, etc., are groups of hundreds that have no tens or ones. Students can represent this with place value (base 10) blocks.



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MCC2.NBT.2 Count within 1000; skip-count by 5s, 10s, and 100s.

This standard calls for students to count within 1,000. This means that students are expected to —count on || from any number and say the next few numbers that come afterwards.

Understand that counting by 2s, 5s and 10s is counting groups of items by that amount.

Example:

What are the next 3 numbers after 498? 499, 500, 501.

When you count back from 201, what are the first 3 numbers that you say? 200, 199, 198. This standard also introduces skip counting by 5s and 100s. Students are introduced to skip counting by 10s in First Grade. Students should explore the patterns of numbers when they skip count. When students skip count by 5s, the ones digit alternates between 5 and 0. When students skip count by 100s, the hundreds digit is the only digit that changes, and it increases by one number.

MCC2.NBT.3 Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.

This standard calls for students to read, write and represent a number of objects with a written numeral (number form or standard form). These representations can include place value (base 10) blocks, pictorial representations or other concrete materials. Please be cognizant that when reading and writing whole numbers, the word "and" should not be used.

Example:

235 is written as two hundred thirty-five.

<u>MCC2.NBT.4 Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using >, =, and < symbols to record the results of comparisons.</u>

This standard builds on the work of MCC2.NBT.1 and MCC2.NBT.3 by having students compare two numbers by examining the amount of hundreds, tens and ones in each number. Students are introduced to the symbols greater than (>), less than (<) and equal to (=) in First Grade, and use them in Second Grade with numbers within 1,000. Students should have ample experiences communicating their comparisons in words before using only symbols in this standard. Example: 452 ___ 455

Student 1

452 has 4 hundreds, 5 tens, and 2 ones. 455 has 4 hundreds, 5 tens, and 5 ones. They have the same number of hundreds and the same number of tens, but 455 has 5 ones and 452 only has 2 ones. 452 is less than 455. 452 < 455.

Student 2

452 is less than 455. I know this because when I count up I say 452 before I say 455. 452 < 455.

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CLUSTER #2: USE PLACE VALUE UNDERSTANDING AND PROPERTIES OF OPERATIONS TO ADD AND SUBTRACT.

Students use their understanding of addition to develop fluency with addition and subtraction within 100. They solve problems within 1000 by applying their understanding of models for addition and subtraction, and they develop, discuss, and use efficient, accurate, and generalizable methods to compute sums and differences of whole numbers in base-ten notation, using their understanding of place value and the properties of operations. They select and accurately apply methods that are appropriate for the context and the numbers involved to mentally calculate sums and differences for numbers with only tens or only hundreds.

MCC2.NBT.5 Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.

This standard mentions the word fluently when students are adding and subtracting numbers within 100. Fluency means accuracy (correct answer), efficiency (basic facts computed within 4-5 seconds), and flexibility (using strategies such as making 10 or breaking numbers apart).

This standard calls for students to use pictorial representations or strategies to find the solution. Students who are struggling may benefit from further work with concrete objects (e.g., place value blocks).

Example: 67 + 25 =____

Place Value Strategy
I broke both 67 and 25
into tens and ones. 6 tens
plus 2 tens equals 8 tens.
Then I added the ones. 7
ones plus 5 ones equals 12
ones. I then combined my
tens and ones. 8 tens plus
12 ones equals 92.
-

Counting On and Decomposing a Number Leading to Ten I wanted to start with 67 and then break 25 apart. I started with 67 and counted on to my next ten. 67 plus 3 gets me to 70. Then I added 2 more to get to 72. I then added my 20 and got to 92. **Commutative Property** I broke 67 and 25 into tens and ones so I had to add 60 + 7 + 20 + 5. I added 60 and 20 first to get 80. Then I added 7 to get 87. Then I added 5 more. My answer is 92.

Example: 63 – 32 = ____

Relationship between Addition and Subtraction

I broke apart both 63 and 32 into tens and ones. I know that 2 plus 1 equals 3, so I have 1 left in the ones place. I know that 3 plus 3 equals 6, so I have a 3 in my tens place. My answer has a 1 in the ones place and 3 in the tens place, so my answer is 31.

MCC2.NBT.6 Add up to four two-digit numbers using strategies based on place value and properties of operations.

This standard calls for students to add a string of two-digit numbers (up to four numbers) by applying place value strategies and properties of operations.

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Example: 43 + 34 + 57 + 24 =____

Student 1: Associative Property

I saw the 43 and 57 and added them first, since I know 3 plus 7 equals 10. When I added them 100 was my answer. Then I added 34 and had 134. Then I added 24 and had 158.

Student 2: Place Value Strategies

I broke up all of the numbers into tens and ones. First I added the tens. 40 + 30 + 50 + 20= 140. Then I added the ones. 3 + 4 + 7 + 4 =18. Then I combined the tens and ones and had 158 as my answer.

Student 3: Place Value Strategies and Associative Property

I broke up all the numbers into tens and ones. First I added up the tens: 40 + 30 + 50 + 20. I changed the order of the numbers to make adding them easier. I know that 30 plus 20 equals 50 and 50 more equals 100. Then I added the 40 and got 140. Then I added up the ones: 3 + 4 + 7 + 4. I changed the order of the numbers to make adding easier. I know that 3 plus 7 equals 10 and 4 plus 4 equals 8. 10 plus 8 equals 18. I then combined my tens and ones. 140 plus 18 equals 158.

MCC2.NBT.7 Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.

This standard builds on the work from 2.NBT.5 by increasing the size of numbers (two 3-digit numbers). Students should have ample experiences to use concrete materials (place value blocks) and pictorial representations to support their work.

This standard also references composing and decomposing a ten. This work should include strategies such as making a 10, making a 100, breaking apart a 10, or creating an easier problem. While the standard algorithm could be used here, students' experiences should extend beyond only working with the algorithm.

Example: 354 + 287 = ____

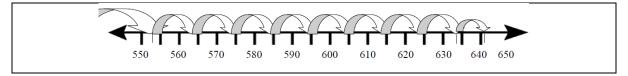
Student 1

I started at 354 and jumped 200. I landed on 554. Then I made 8 jumps of 10 and landed on 634. I then jumped 7 and landed on 641

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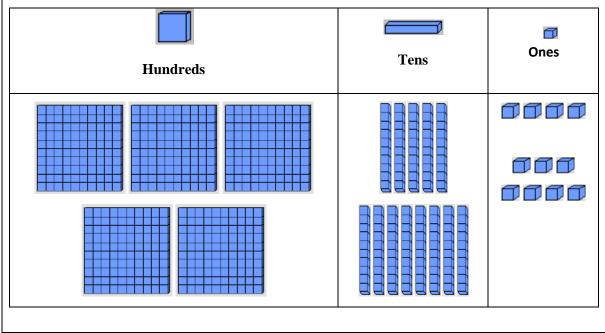
Student 2

I broke all of the numbers up by place using a place value chart. I first added the ones.4 + 7 = 11. I then added the tens. 50 + 80 = 130. I then added the hundreds. 300 + 200 = 500. I then combined my answers. 500 + 130 = 630. 630 + 11 = 641

Student 2

I broke all of the numbers up by place using a place value chart.

- I first added the ones: 4 + 7 = 11.
- Then I added the tens: 50 + 80 = 130.
- Then I added the hundreds: 300 + 200 = 500.
- Then I combined my answers: 500 + 130 = 630; 630 + 11 = 641.



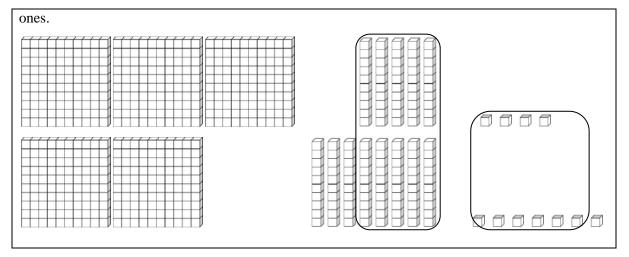
Student 3

I used place value blocks. I made a pile of 354. I then added 287. That gave me 5 hundreds, 13 tens and 11 ones. I noticed that I could trade some pieces. I had 11 ones, and I traded 10 ones for a ten. I then had 14 tens, so I traded 10 tens for a hundred. I ended up with 6 hundreds, 4 tens, and 1

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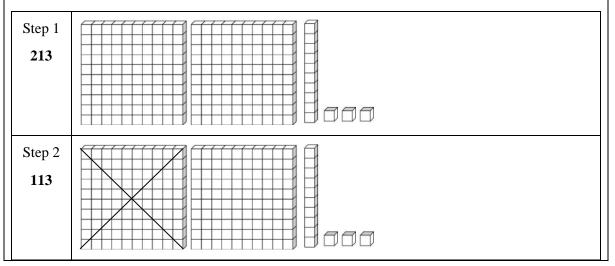
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Example: 213 – 124 = ____

Student 1

I used place value blocks. I made a pile of 213. Then I started taking away blocks. First I took away a hundred, which left me with 1 hundred and thirteen. I need to take away 2 tens but I only had 1 ten so I traded in my last hundred for 10 tens. Then I took 2 tens away, leaving me with no hundreds, 9 tens, and 3 ones. Then I had to take 4 ones away but I only have 3 ones. I traded in a ten for 10 ones. Then I took away 4 ones. This left me with no hundreds, 8 tens, and 9 ones. My answer is 89.



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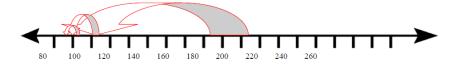
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Step 3 93	
Step 4 89	
Final Answer 89	

Student 2

I started at 213 and moved backwards 100 and landed on 113. Then I moved back 2 jumps of ten and landed on 93. Then I moved back 4 and landed on 89.



Student 3

I noticed that I was taking 124 away from 213. I changed 213 into 224 by adding 11. That made my problem 224 - 124. I know the answer to that problem is 100. Then I had to take away the 11 that I added. 100 - 11 = 89. My answer is 89.

MCC2.NBT.8 Mentally add 10 or 100 to a given number 100–900, and mentally subtract 10 or 100 from a given number 100–900.

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This standard calls for students to mentally add or subtract multiples of 10 or 100 to any number between 100 and 900. Students should have ample experiences working with the concept that when you add or subtract multiples of 10 or 100 that you are only changing the tens place (multiples of ten) or the digit in the hundreds place (multiples of 100).

In this standard, problems in which students cross centuries should also be considered. Example: 273 + 60 = 333.

<u>MCC2.NBT.9 Explain why addition and subtraction strategies work, using place value and the properties of operations.</u>

This standard calls for students to explain using concrete objects, pictures and words (oral or written) to explain why addition or subtraction strategies work. The expectation is that students apply their knowledge of place value and the properties of operations in their explanation. Students should have the opportunity to solve problems and then explain why their strategies work.

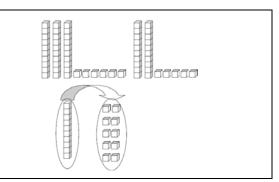
Example: There are 36 birds in the park. 25 more birds arrive. How many birds are there? Solve the problem and show your work.

Student 1

I broke 36 and 25 into tens and ones and then added them. 30 + 6 + 20 + 5. I can change the order of my numbers, so I added 30 + 20 and got 50. Then I added on 6 to get 56. Then I added 5 to get 61. This strategy works because I broke all the numbers up by their place value.

Student 2

I used place value blocks and made a pile of 36. Then I added 25. I had 5 tens and 11 ones. I had to trade 10 ones for 1 10. Then I had 6 tens and 1 one. That makes 61. This strategy works because I added up the tens and then added up the ones and traded if I had more than 10 ones.



Students could also have experiences examining strategies and explaining why they work. Also include incorrect examples for students to examine.

Example: One of your classmates solved the problem 56 - 34 =____ by writing —I know that I need to add 2 to the number 4 to get 6. I also know that I need to add 20 to 30 to get 20 to get to 50. So, the answer is 22. Is their strategy correct? Explain why or why not?

Example: One of your classmates solved the problem 25 + 35 by adding 20 + 30 + 5 + 5. Is their strategy correct? Explain why or why not?

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MEASUREMENT AND DATA (MD)

CLUSTER #1: MEASURE AND LENGTHS IN STANDARD UNITS.

Students recognize the need for standard units of measure (centimeter and inch) and they use rulers and other measurement tools with the understanding that linear measure involves an iteration of units. They recognize that the smaller the unit, the more iterations they need to cover a given length.

<u>MCC2.MD.1</u> Measure the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes.

This standard calls for students to measure the length of objects in both customary (inches and feet) and metric (centimeters and meters). Students should have ample experiences choosing objects, identifying the appropriate tool and unit, and then measuring the object. The teacher should allow students to determine which tools and units to use.

Foundational understandings to help with measure concepts:

- Understand that larger units can be subdivided into equivalent units (partition).
- Understand that the same unit can be repeated to determine the measure (iteration).
- Understand the relationship between the size of a unit and the number of units needed (compensatory principle).
- Understand the measuring of two-dimensional space (area) using non-standard units.

MCC2.MD.2 Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen. This standard calls for students to measure an object using two units of different lengths.

Example: A student measures the length of their desk and finds that it is 3 feet and 36 inches. Students should explore the idea that the length of the desk is larger in inches than in feet, since inches are smaller units than feet. This concept is referred to as the compensatory principle. Note: this standard does not specify whether the units have to be within the same system.

MCC2.MD.3 Estimate lengths using units of inches, feet, centimeters, and meters.

This standard calls for students to estimate the lengths of objects using inches, feet, centimeters, and meters. Students should make estimates after seeing a benchmark unit, such as the length of one inch, before making their estimate.

Example: Look at your ruler to see how long one inch is. Now, estimate the length of this paper in inches.

<u>MCC2.MD.4 Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit.</u>

This standard calls for students to determine the difference in length between two objects. Students should choose objects, identify appropriate tools and units, measure both objects, and then determine the differences in lengths.

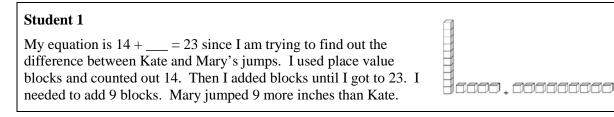
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CLUSTER #2: RELATE ADDITION AND SUBTRACTION TO LENGTH.

<u>MCC2.MD.5</u> Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.

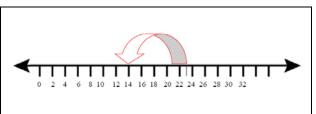
This standard applies the concept of length to solve addition and subtraction word problems with numbers within 100. Students should use the same unit in these problems.

Example: In P.E. class Kate jumped 14 inches. Mary jumped 23 inches. How much farther did Mary jump than Kate? Write an equation and then solve the problem.



Student 2

My equation is 23 - 14 =_____. I drew a number line. I started at 23. I moved back to 14 and counted how far I moved. I moved back 9 spots. Mary jumped 9 more inches than Kate.



MCC2.MD.6 Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers 0, 1, 2, ..., and represent whole-number sums and differences within 100 on a number line diagram.

This standard calls for students to create number lines using numbers within 100 to solve addition and subtraction problems. Students should create the number line with evenly spaced points corresponding to the numbers.

CLUSTER #3: WORK WITH TIME AND MONEY.

MCC2.MD.7 Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m.

This standard calls for students to tell (orally and in writing) and write time after reading analog and digital clocks. Time should be to 5 minute intervals, and students should also use the terms a.m. and p.m. Teachers should help students make the connection between skip counting by 5s (MCC2.NBT.2) and telling time on an analog clock.

MCC2.MD.8 Solve word problems involving dollar bills, quarters, dimes, nickels, and pennies, using \$ and \$ symbols appropriately. Example: If you have 2 dimes and 3 nonnies, how many cents do you

using \$ and ¢ symbols appropriately. *Example: If you have 2 dimes and 3 pennies, how many cents do you have?*

This standard calls for students to solve word problems involving either dollars or cents. Since students have not been introduced to decimals, problems should either have only dollars or only cents.

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Example: What are some possible combinations of coins (pennies, nickels, dimes, and quarters) that equal 37 cents?

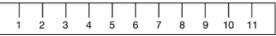
Example: What are some possible combinations of dollar bills (\$1, \$5 and \$10) that equal 12 dollars?

CLUSTER #4: REPRESENT AND INTERPRET DATA.

<u>MCC2.MD.9 Generate measurement data by measuring lengths of several objects to the nearest</u> whole unit, or by making repeated measurements of the same object. Show the measurements by making a line plot, where the horizontal scale is marked off in whole-number units.

This standard calls for students to represent the length of several objects by making a line plot. Students should round their lengths to the nearest whole unit.

Example: Measure objects in your desk to the nearest inch, display data collected on a line plot. How many objects measured 2 inches? 3 inches? Which length had the most number of objects? How do you know?



<u>MCC2.MD.10</u> Draw a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. Solve simple put-together, take-apart, and compare problems using information presented in a bar graph.

This standard calls for students to work with categorical data by organizing, representing and interpreting data. Students should have experiences posing a question with 4 possible responses and then work with the data that they collect.

Example: Students pose a question and the 4 possible responses. Which is your favorite flavor of ice cream: Chocolate, vanilla, strawberry, or cherry?

Students collect their data by using tallies or another way of keeping track. Students organize their data by totaling each category in a chart or table. Picture and bar graphs are introduced in 2nd Grade.

	Flavor	Number of People
Chocolate		12
Vanilla		5
Strawberry		6

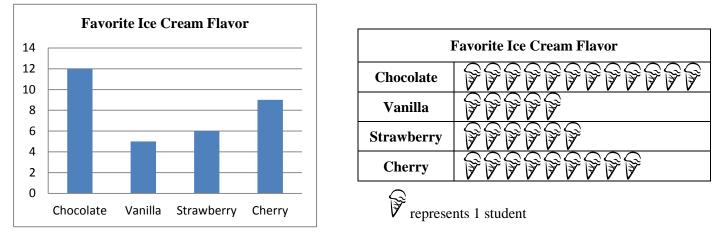
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Cherry	9

Students display their data using a picture graph or bar graph using a single unit scale.



Students answer simple problems related to addition and subtraction that ask them to put together, take apart, and compare numbers. See Table 1 at the end of this document for examples of these.

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GEOMETRY (G)

CLUSTER #1: REASON WITH SHAPES AND THEIR ATTRIBUTES.

Students describe and analyze shapes by examining their sides and angles. Students investigate, describe, and reason about decomposing and combining shapes to make other shapes. Through building, drawing, and analyzing two- and three-dimensional shapes, students develop a foundation for understanding area, volume, congruence, similarity, and symmetry in later grades.

<u>MCC2.G.1 Recognize and draw shapes having specified attributes, such as a given number of</u> angles or a given number of equal faces. Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.

This standard calls for students to identify (recognize) and draw shapes based on a given set of attributes. These include triangles, quadrilaterals (squares, rectangles, and trapezoids), pentagons, hexagons and cubes.

Example: Draw a closed shape that has five sides. What is the name of the shape?

Student 1

I drew a shape with 5 sides. It is called a pentagon.

MCC2.G.2 Partition a rectangle into rows and columns of same-size squares and count to find the total number of them.

This standard calls for students to partition a rectangle into squares (or square-like regions) and then determine the total number of squares. This relates to the standard 2.OA.4 where students are arranging objects in an array of rows and columns.

Example: Split the rectangle into 2 rows and 4 columns. How many small squares did you make?

MCC2.G.3 Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape.

This standard calls for students to partition (split) circles and rectangles into 2, 3 or 4 equal shares (regions). Students should be given ample experiences to explore this concept with paper strips and pictorial representations. Students should also work with the vocabulary terms halves, thirds, half of, third of, and fourth (or quarter) of. While students are working on this standard, teachers should help them to make the connection that a —whole|| is composed of two halves, three thirds, or four fourths. This standard also addresses the idea that equal shares of identical wholes may not have the same shape.

Example: Divide each rectangle into fourths a different way.

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ARC OF LESSON (OPENING, WORK SESSION, CLOSING)

"When classrooms are workshops-when learners are inquiring, investigating, and constructing- there is already a feeling of community. In workshops learners talk to one another, ask one another questions, collaborate, prove, and communicate their thinking to one another. The heart of math workshop is this: investigations and inquiries are ongoing, and teachers try to find situations and structure contexts that will enable children to mathematize their lives- that will move the community toward the horizon. Children have the opportunity to explore, to pursue inquiries, and to model and solve problems on their own creative ways. Searching for patterns, raising questions, and constructing one's own models, ideas, and strategies are the primary activities of math workshop. The classroom becomes a community of learners engaged in activity, discourse, and reflection." *Young Mathematicians at Work- Constructing Addition and Subtraction* by Catherine Twomey Fosnot and Maarten Dolk.

"Students must believe that the teacher does not have a predetermined method for solving the problem. If they suspect otherwise, there is no reason for them to take risks with their own ideas and methods." *Teaching Student-Centered Mathematics, K-3* by John Van de Walle and Lou Ann Lovin.

Opening: Set the stage

Get students mentally ready to work on the task Clarify expectations for products/behavior How?

- Begin with a simpler version of the task to be presented
- Solve problem strings related to the mathematical idea/s being investigated
- Leap headlong into the task and begin by brainstorming strategies for approaching the task
- Estimate the size of the solution and reason about the estimate

Make sure everyone understands the task before beginning. Have students restate the task in their own words. Every task should require more of the students than just the answer.

Work session: Give 'em a chance

Students- grapple with the mathematics through sense-making, discussion, concretizing their mathematical ideas and the situation, record thinking in journals

Teacher- Let go. Listen. Respect student thinking. Encourage testing of ideas. Ask questions to clarify or provoke thinking. Provide gentle hints. Observe and assess.

Closing: Best Learning Happens Here

Students- share answers, justify thinking, clarify understanding, explain thinking, question each other Teacher- Listen attentively to all ideas, ask for explanations, offer comments such as, "Please tell me how you figured that out." "I wonder what would happen if you tried..." Anchor charts

Read Van de Walle K-3, Chapter 1

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BREAKDOWN OF A TASK (UNPACKING TASKS)

How do I go about tackling a task or a unit?

- Read the unit in its entirety. Discuss it with your grade level colleagues. Which parts do you feel comfortable with? Which make you wonder? Brainstorm ways to implement the tasks. Collaboratively complete the culminating task with your grade level colleagues. As students work through the tasks, you will be able to facilitate their learning with this end in mind. The structure of the units/tasks is similar task to task and grade to grade. This structure allows you to converse in a vertical manner with your colleagues, school-wide. The structure of the units/tasks is similar task to grade. There is a great deal of mathematical knowledge and teaching support within each grade level guide, unit, and task.
- 2. Read the first task your students will be engaged in. Discuss it with your grade level colleagues. Which parts do you feel comfortable with? Which make you wonder? Brainstorm ways to implement the tasks.
- 3. If not already established, use the first few weeks of school to establish routines and rituals, and to assess student mathematical understanding. You might use some of the tasks found in the unit, or in some of the following resources as beginning tasks/centers/math tubs which serve the dual purpose of allowing you to observe and assess.

Additional Resources:

Math Their Way: <u>http://www.center.edu/MathTheirWay.shtml</u> NZMaths- <u>http://www.nzmaths.co.nz/numeracy-development-projects-books?parent_node</u>= K-5 Math Teaching Resources- <u>http://www.k-5mathteachingresources.com/index.html</u> (this is a for-profit site with several free resources) Winnepeg resources- <u>http://www.wsd1.org/iwb/math.htm</u> Math Solutions- <u>http://www.mathsolutions.com/index.cfm?page=wp9&crid=56</u>

- 4. Points to remember:
 - Each task begins with a list of the standards specifically addressed in that task, however, that does not mean that these are the only standards addressed in the task. Remember, standards build on one another, and mathematical ideas are connected.
 - Tasks are made to be modified to match your learner's needs. If the names need changing, change them. If the materials are not available, use what is available. If a task doesn't go where the students need to go, modify the task or use a different resource.
 - The units are not intended to be all encompassing. Each teacher and team will make the units their own, and add to them to meet the needs of the learners.

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ROUTINES AND RITUALS

Teaching Math in Context and Through Problems

"By the time they begin school, most children have already developed a sophisticated, informal understanding of basic mathematical concepts and problem solving strategies. Too often, however, the mathematics instruction we impose upon them in the classroom fails to connect with this informal knowledge" (Carpenter et al., 1999). The 8 Standards of Mathematical Practices (SMP) should be at the forefront of every mathematics lessons and be the driving factor of HOW students learn.

One way to help ensure that students are engaged in the 8 SMPs is to construct lessons built on context or through story problems. "Fosnot and Dolk (2001) point out that in story problems children tend to focus on getting the answer, probably in a way that the teacher wants. "Context problems, on the other hand, are connected as closely as possible to children's lives, rather than to 'school mathematics'. They are designed to anticipate and to develop children's mathematical modeling of the real world."

Traditionally, mathematics instruction has been centered around a lot of problems in a single math lesson, focusing on rote procedures and algorithms which do not promote conceptual understanding. Teaching through word problems and in context is difficult however, "kindergarten students should be expected to solve word problems" (Van de Walle, K-3).

A *problem* is defined as any task or activity for which the students have no prescribed or memorized rules or methods, nor is there a perception by students that there is a specific correct solution method. A problem for learning mathematics also has these features:

- The problem must begin where the students are which makes it accessible to all learners.
- The problematic or engaging aspect of the problem must be due to the mathematics that the students are to learn.
- The problem must require justifications and explanations for answers and methods.

It is important to understand that mathematics is to be taught *through* problem solving. That is, problem-based tasks or activities are the vehicle through which the standards are taught. Student learning is an outcome of the problem-solving process and the result of teaching within context and through the Standards for Mathematical Practice. (Van de Walle and Lovin, Teaching Student-Centered Mathematics: K-3, page 11).

Use of manipulatives

"It would be difficult for you to have become a teacher and not at least heard that the use of manipulatives, or a "hands-on approach," is the recommended way to teach mathematics. There is no doubt that these materials can and should play a significant role in your classroom. Used correctly they can be a positive factor in children's learning. But they are not a cure-all that some educators seem to believe them to be. It is important that you have a good perspective on how manipulatives can help or fail to help children construct ideas. We can't just give students a ten-frame or bars of Unifix cubes and expect them to develop the mathematical ideas that these manipulatives can potentially represent. When

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a new model of new use of a familiar model is introduced into the classroom, it is generally a good idea to explain how the model is used and perhaps conduct a simple activity that illustrates this use." (Van de Walle and Lovin, Teaching Student-Centered Mathematics: K-3, page 6).

Once you are comfortable that the models have been explained, you should not force their use on students. Rather, students should feel free to select and use models that make sense to them. In most instances, not using a model at all should also be an option. The choice a student makes can provide you with valuable information about the level of sophistication of the student's reasoning.

Whereas the free choice of models should generally be the norm in the classroom, you can often ask students to model to show their thinking. This will help you find out about a child's understanding of the idea and also his or her understanding of the models that have been used in the classroom.

The following are simple rules of thumb for using models:

- Introduce new models by showing how they can represent the ideas for which they are intended.
- Allow students (in most instances) to select freely from available models to use in solving problems.
- Encourage the use of a model when you believe it would be helpful to a student having difficulty." (Van de Walle and Lovin, Teaching Student-Centered Mathematics: K-3, page 8-9)

Use of strategies and effective questioning

Teachers ask questions all the time. They serve a wide variety of purposes: to keep learners engaged during an explanation; to assess their understanding; to deepen their thinking or focus their attention on something. This process is often semi-automatic. Unfortunately, there are many common pitfalls. These include:

- asking questions with no apparent purpose;
- asking too many closed questions;
- asking several questions all at once;
- poor sequencing of questions;
- asking rhetorical questions;
- asking 'Guess what is in my head' questions;
- focusing on just a small number of learners;
- ignoring incorrect answers;
- not taking answers seriously.

In contrast, the research shows that effective questioning has the following characteristics:

- Questions are planned, well ramped in difficulty.
- Open questions predominate.
- A climate is created where learners feel safe.
- A 'no hands' approach is used, for example when all learners answer at once using miniwhiteboards, or when the teacher chooses who answers.

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- Probing follow-up questions are prepared.
- There is a sufficient 'wait time' between asking and answering a question.
- Learners are encouraged to collaborate before answering.
- Learners are encouraged to ask their own questions.

There are many types of questioning that promote mathematical thinking. On these pages we can offer a sample of what can be done.

0-99 Chart or 1-100 Chart

(Adapted information from About Teaching Mathematics A K–8 RESOURCE MARILYN BURNS 3rd edition and Van de Walle)

Both the 0-99 Chart and the 1-100 Chart are valuable tools in the understanding of mathematics. Most often these charts are used to reinforce counting skills. Counting involves two separate skills: (1) ability to produce the standard list of counting words (i.e. one, two, three) and (2) the ability to connect the number sequence in a one-to-one manner with objects (Van de Walle, 2007). The counting sequence is a rote procedure. The ability to attach meaning to counting is "the key conceptual idea on which all other number concepts are developed" (Van de Walle, p. 122). Children have greater difficulty attaching meaning to counting than rote memorization of the number sequence. Although both charts can be useful, the focus of the 0-99 chart should be at the forefront of number sense development in early elementary.

A 0-99 Chart should be used in place of a 1-100 Chart when possible in early elementary mathematics for many reasons, but the overarching argument for the 0-99 is that it helps to develop a deeper understanding of place value. Listed below are some of the benefits of using the 0-99 Chart in your classroom:

- A 0-99 Chart begins with zero where as a hundred's chart begins with 1. It is important to include zero because it is a digit and just as important as 1-9.
- A 1-100 chart puts the decade numerals (10, 20, 30, etc.) on rows without the remaining members of the same decade. For instance, on a hundred's chart 20 appears at the end of the teens' row. This causes a separation between the number 20 and the numbers 21-29. The number 20 is the beginning of the 20's family; therefore it should be in the beginning of the 20's row like in a 99's chart to encourage students to associate the quantities together.
- A 0-99 chart ends with the last two digit number, 99, this allows the students to concentrate their understanding using numbers only within the ones' and tens' place values. A hundred's chart ends in 100, introducing a new place value which may change the focus of the places.
- The understanding that 9 units fit in each place value position is crucial to the development of good number sense. It is also very important that students recognize that zero is a number, not merely a placeholder. This concept is poorly modeled by a typical 1-100 chart, base ten manipulatives, and even finger counting. We have no "zero" finger, "zero" block, or "zero" space on typical 1-100 number charts. Whereas having a zero on the chart helps to give it status and reinforces that zero holds a quantity, a quantity of none. Zero is the answer to a question such as, "How many elephants are in the room?".

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• Including zero presents the opportunity to establish zero correctly as an even number, when discussing even and odd. Children see that it fits the same pattern as all of the other even numbers on the chart.

0	1	2	3	4	5	6	7	8	9
10	11	12	13	14	15	16	17	18	19
20	21	22	23	24	25	26	27	28	29
30	31	32	33	34	35	36	37	38	39
40	41	42	43	44	45	46	47	48	49
50	51	52	53	54	55	56	57	58	59
60	61	62	63	64	65	66	67	68	69
70	71	72	73	74	75	76	77	78	79
80	81	82	83	84	85	86	87	88	89
90	91	92	93	94	95	96	97	98	99

While there are differences between the 0-99 Chart and the 1-100 Chart, both number charts are valuable resources for your students and should be readily available in several places around the classroom. Both charts can be used to recognize number patterns, such as the increase or decrease by multiples of ten. Provide students the opportunity to explore the charts and communicate the patterns they discover.

The number charts should be placed in locations that are easily accessible to students and promote conversation. Having one back at your math calendar/bulletin board area provides you the opportunity to use the chart to engage students in the following kinds of discussions. Ask students to find the numeral that represents:

- the day of the month
- the month of the year
- the number of students in the class
- the number of students absent or any other amount relevant to the moment.

Using the number is 21, give directions and/or ask questions similar to those below.

- Name a number greater than 21.
- Name a number less than 21.
- What number is 3 more than/less than 21?
- What number is 5 more than/less than 21?
- What number is 10 more than/less than 21?
- Is 21 even or odd?
- What numbers live right next door to 21?

Ask students to pick an even number and explain how they know the number is even. Ask students to pick an odd number and explain how they know it is odd. Ask students to count by 2's, 5's or 10's. Tell them to describe any patterns that they see. (Accept any patterns that students are able to justify. There are many right answers!)

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Number Lines

The use of number lines in elementary mathematics is crucial in students' development of number and mathematical proficiency. While the CCGPS explicitly state use number lines in grades 2-5, number lines should be used in all grade levels and in multiple settings.

According to John Van de Walle,

A number line is also a worthwhile model, but can initially present conceptual difficulties for children below second grade and students with disabilities (National Research Council Committee, 2009) This is partially due to their difficulty in seeing the unit, which is a challenge when it appears in a continuous line. A number line is also a shift from counting a number of individual objects in a collection to continuous length units. There are, however, ways to introduce and model number lines that support young learners as they learn this representation. Familiarity with a number line is essential because third grade students will use number lines to locate fractions and add and subtract time intervals, fourth graders will locate decimals and use them for measurement, and fifth graders will use perpendicular number lines in coordinate grids (CCSSO,2010).

A number line measures distance from zero the same way a ruler does. If you don't actually teach the use of the number line through emphasis on the unit (length), students may focus on the hash marks or numerals instead of the spaces (a misunderstanding that becomes apparent when their answers are consistently off by one). At first students can build a number path by using a given length, such as a set of Cuisenaire rods of the same color to make a straight line of multiple single units (Van de Walle and Lovin, Teaching Student-Centered Mathematics: 3-5 pg. 106-107)

Open number lines are particularly useful for building students' number sense. They can also form the basis for discussions that require the precise use of vocabulary and quantities, and are therefore a good way to engage students in the Standards for Mathematical Practice.

While the possibilities for integrating number lines into the mathematics classroom are endless, the following are some suggestions/ideas:

- On a bulletin board, attach a string which will function as an open number line. Each morning (or dedicated time for math routines) put a new number on each student's desk. Using the some type of adhesive (thumb tack, tape, etc.), students will place the number in the appropriate location on the string. In the beginning of the year, provide students with numbers that are more familiar to them. As the year progresses, move through more complex problems such as skip counting, fractions, decimals or other appropriate grade level problems. Through daily integration, the number line becomes part of the routine. Following the number placement, have a brief discussion/debriefing of the reasoning used by students to place the numbers.
- In the 3-Act tasks placed throughout the units, students will be provided opportunities to use an open number line to place estimates that are too low, too high and just right as related to the posed problem. Similar opportunities can also be used as part of a daily routine.

Math Maintenance Activities

In addition to instruction centered on the current unit of study, the math instructional block should include time devoted to reviewing mathematics that have already been taught, previewing upcoming mathematics, and developing mental math and estimation skills. There is a saying that if you don't use it, you'll lose it. If students don't have opportunities to continuously apply and refine the math skills they've learned previously, then they may forget how to apply what they've learned. Unlike vocabulary words for literacy, math vocabulary words are not used much outside math class, so it becomes more important to use those words in discussions regularly. Math maintenance activities incorporate review and preview of math concepts and vocabulary and help students make connections across domains. It's recommended that 15 to 30 minutes of the math instructional block be used for these math maintenance activities each day. It's not necessary nor is it recommended that teachers do every activity every day. Teachers should strive for a balance of math maintenance activities so that over the course of a week, students are exposed to a variety of these activities. Math maintenance time may occur before or after instruction related to the current math unit, or it can occur at a different time during the day.

The goals of this maintenance time should include:

- Deepening number sense, including subitizing, flexible grouping of quantities, counting forward and backward using whole numbers, fractions, decimals and skip counting starting at random numbers or fractional amounts
- Developing mental math skills by practicing flexible and efficient numerical thinking through the use of operations and the properties of operations
- Practicing estimation skills with quantities and measurements such as length, mass, and liquid volume, depending on grade level
- Practicing previously-taught skills so that students deepen and refine their understanding
- Reviewing previously-taught concepts that students struggled with as indicated on their assessments, including gaps in math concepts taught in previous grade levels
- Using a variety of math vocabulary terms, especially those that are used infrequently
- Practicing basic facts using strategies learned in previous grade levels or in previous units to develop or maintain fluency
- Previewing prerequisite skills for upcoming math units of study
- Participating in mathematical discussions with others that require students to construct viable arguments and critique the reasoning of others

To accomplish these goals, math maintenance activities can take many different forms. Some activities include:

- Number Corner or Calendar Time
- Number Talks

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- Estimation Activities/Estimation 180
- Problem of the Day or Spiraled Review Problems

In addition, math discussions, math journals and math games are appropriate not only for the current unit of study, but also for maintaining math skills that were previously taught.

Although there are commercially-available materials to use for math maintenance activities, there are also many excellent websites and internet resources that are free for classroom use. Here is a partial list of some recommended resources. A more detailed explanation of some of these components follows below.

Math Maintenance Activity	Possible Resources				
Number Corner or Calendar Time	 <u>http://teachelemmath.weebly.com/calendar.html</u> Every Day Counts Calendar Math from Houghton Mifflin Harcourt Number Corner from The Math Learning Center <u>Number Talks</u> by Sherry Parrish 				
Estimation Activities/Estimation 180	<u>http://www.estimation180.com/</u>				
Problem of the Day/Spiraled Review Problems	 www.insidemathematics.org http://nzmaths.co.nz/teaching-material http://www.k-5mathteachingresources.com/ http://mathlearnnc.sharpschool.com/cms/One.aspx?portalld=4507 283&pageId=5856325 Children's Mathematics: Cognitively Guided Instruction by Thomas Carpentar, et. Al. <u>Extending Children's Mathematics: Fractions and Decimals</u> by Epson and Levi 				

Number Corner/Calendar Time

Number Corner is a time set aside to go over mathematics skills (Standards for calendar can be found in Social Studies) during the primary classroom day. This should be an interesting and motivating time for students. A calendar board or corner can be set up and there should be several elements that are put in place. The following elements should be set in place for students to succeed during Number Corner:

- 1. a safe environment
- 2. concrete models or math tools
- 3. opportunities to think first and then discuss
- 4. student interaction

Number Corner should relate several mathematics concepts/skills to real life experiences. This time can be as simple as reviewing the months, days of the week, temperature outside, and the schedule for the day, but some teachers choose to add other components that integrate more standards. Number Corner should be used as a time MATHEMATICS • GRADE 2• Grade Level Overview

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to engage students in a discussion about events which can be mathematized, or as a time to engage in Number Talks.

- Find the number _____.
- If I have a nickel and a dime, how much money do I have? (any money combination)
- What is ____ more than ____?
- What is ____ less than ____?
- Mystery number: Give clues and they have to guess what number you have.
- This number has _____tens and _____ ones. What number am I?
- What is the difference between ____ and ____?
- What number comes after ____? before ___?
- Tell me everything you know about the number _____. (Anchor Chart)

Number Corner is also a chance to familiarize your students with Data Analysis. This creates an open conversation to compare quantities, which is a vital process that must be explored before students are introduced to addition and subtraction.

- At first, choose questions that have only two mutually exclusive answers, such as yes or no (e.g., Are you a girl or a boy?), rather than questions that can be answered yes, no, or maybe (or sometimes). This sets up the part-whole relationship between the number of responses in each category and the total number of students present and it provides the easiest comparison situation (between two numbers; e.g., Which is more? How much more is it?). Keep in mind that the concept of less than (or fewer) is more difficult than the concept of greater than (or more). Be sure to frequently include the concept of less in your questions and discussions about comparisons.
- Later, you can expand the questions so they have more than two responses. Expected responses may include maybe, I'm not sure, I don't know or a short, predictable list of categorical responses (e.g., In which season were you born?).
- Once the question is determined, decide how to collect and represent the data. Use a variety of approaches, including asking students to add their response to a list of names or tally marks, using Unifix cubes of two colors to accumulate response sticks, or posting 3 x 5 cards on the board in columns to form a bar chart.
- The question should be posted for students to answer. For example, "Do you have an older sister?" Ask students to contribute their responses in a way that creates a simple visual representation of the data, such as a physical model, table of responses, bar graph, etc.
- Each day, ask students to describe, compare, and interpret the data by asking questions such as these: "What do you notice about the data? Which group has the most? Which group has the least? How many more answered [this] compared to [that]? Why do you suppose more answered [this]?" Sometimes ask data gathering questions: "Do you think we would get similar data on a different day? Would we get similar data if we asked the same question in another class? Do you think these answers are typical for first graders? Why or why not?"
- Ask students to share their thinking strategies that justify their answers to the questions. Encourage and reward attention to specific details. Focus on relational thinking and problem solving strategies for making comparisons. Also pay attention to identifying part-whole relationships; and reasoning that leads to interpretations.
- Ask students questions about the ideas communicated by the representation used. What does this graph represent? How does this representation communicate this information clearly? Would a different representation communicate this idea better?
- The representation, analysis, and discussion of the data are the most important parts of the routine (as opposed to the data gathering process or the particular question being asked). These mathematical

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processes are supported by the computational aspects of using operations on the category totals to solve part-whole or "compare" problems.

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Number Talk Taken from Oakland Unified School District OUSD Math Instructional Toolkit

Purpose: flexibility, accuracy and efficiency in mathematical thinking through the articulation of and sharing of mental math strategies

GENERAL DESCRIPTION:

A Number Talk is a 10 to 15 minute whole group mental math activity where students find the answer to a math problem in their heads, then share aloud the strategies they used to find that answer. This strategy helps to develop quality student discourse in a whole class setting as students are encouraged to explain their thinking, justify their reasoning, and make sense of each other's strategies.

During a Number Talk, the teacher steps away from his/her role of authority, and into the role of facilitator by asking students questions, recording student responses on the board, and encouraging students to make meaning out of the mathematics through verbal exchange.

A Number Talk can be used to address gaps in student skills or understanding, to confront anticipated misconceptions, to surface multiple strategies, and/or as a formative assessment when introducing new concepts. Number Talks also build flexibility, accuracy and efficiency with numbers for all students.

In lower elementary, students might experience a Number Talk where they have to look at a pattern of dots for 3 seconds, and share strategies for how they knew the total number of dots. In upper elementary, students may be asked to multiply 25 × 8 and may use different decomposition strategies or their knowledge of money to calculate. In middle school, students may be asked to mentally find 35% of 160. In high school, they may share multiple strategies for solving 1252/3 • 2. Number Talks may be used to make sense of grade-level content, but can also build from concepts from previous classes by starting with a dot talk or a simple arithmetic problem at any grade, based on where the students' needs are.

WHEN AND WHY IS THIS USEFUL?	WHAT CAN STUDENTS LEARN FROM THIS
 A Number Talk is useful: To help students move from a reliance on memorization to truly understanding numbers and their relationships to each other. To help students recognize structure, and use that structure to understand more complex mathematics. As a regular routine where the problems in a series of Number Talks build on each other. To launch a task by activating students' prior knowledge. To provide students the opportunity to practice explaining their thinking and asking each other questions. To develop a stronger sense of mathematical identity and self-confidence in students, since mistakes are treated as learning opportunities, and everyone's opinion contributes to group knowledge. 	 about the strategies used to solve a problem. Ease with composing and decomposing numbers Conceptual understanding of the relationships between numbers Computation strategies Mathematical reasoning skills Precision in explanations of mathematical thinking Multiple strategies and multiple representations for finding an answer Learning from the ideas of peers Confidence and motivation, contributing to a

Number Talk: Step-by-Step

Ready to try a Number Talk? Here are step-by-step instructions for structuring a Number Talk in a lesson. 1. Start by identifying the mathematics students will need to be successful in a curricular unit. Are there basic mathematical structures or patterns that, if recognized and understood by students, will lead to understanding of more complex mathematics? Would familiarity and flexibility with particular understandings about numbers, or kinds of computations, support students to make connections between the new material and things they have learned previously? Are there basic skills students may lack that might hinder their progress with new material? From this list, write a problem that students can tackle mentally and to which they might apply several different solving strategies. (See "Choosing a Problem," below.)

2. Anticipate the different strategies that students might apply to finding an answer to the question. Consider how to record each of these strategies so that the symbols or diagrams accurately reflect the strategy. This can be one of the most challenging parts of facilitating a Number Talk, but is critical. Scribing in a way that accurately represents students' thinking allows students to see the structure of their thinking and to compare different strategies.

3. Before posing the question to the class, remind students that this is a mental math exercise, and that everyone will have time to arrive at an answer silently before the discussion begins. If they arrive at an answer before the silent time is up, they should try to think of a different strategy for finding the answer. Demonstrate any silent signals you want students to use to indicate when they are ready – such as putting a fist to their chest when they have an answer, and raising a finger for each additional strategy they think of.

4. Surface the different answers students reached. Poll the class to determine if most students got a specific answer. Then, call on students to share strategies and record their solving processes. As much as possible, based on the complexity of the problem and the strategy, listen through a student's full explanation before scribing, so that the strategy can be accurately represented and you can avoid assuming or prompting a next step by how initial numbers are recorded.

5. Wrap up the number talk. Closure can be achieved, through a discussion, such as identifying similarities and differences between strategies, or by connecting the number talk to the material of the unit, or by asking students to apply a strategy different from their own to a new problem.

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Choosing a Problem

A Number Talk may stand alone in a unit as a way to activate specific prior knowledge or introduce new content, or Number Talks may be organized in a series over several lessons in order to point to particular structures in numbers and expressions.

The problem that a Number Talk is organized around may take different forms. Examples include: Solve or evaluate an expression: 53+37=?

"Simplify 50000/150"

Compare two values:

"Determine which is greater: 2/3 or 10/18"

Consider a string of computations to identify patterns:

 $2 \times 30 = 60$ $3 \times 30 = 90$ $4 \times 30 = 120$ $5 \times 30 = 150$ $6 \times 30 = ?$

How many dots are there? How did you see the dots?

·· .

When crafting a problem as the focus of a number talk, consider:

- Does the problem lend itself to mental math? Numbers should be friendly enough to manipulate without pencil and paper. If multiple steps are required, the numbers should be easy to retain as students process through the math.
- Are there multiple strategies for solving the problem? Some problems may be able to be visualized in multiple ways (geometrically, on a number line, on a graph, with an expression, using friendly numbers). Numbers may be able to be composed or decomposed in different ways to achieve an answer. If you cannot readily find two or three different ways to arrive at an answer, the problem may not stimulate multiple strategies or discussion from students.
- If the Number Talk falls in a series, does it allow students to build on the strategies used in the previous Number Talk? Do multiple strategies translate to the new problem? Are all of the strategies applicable in the new context, and is there a value to reasoning about why or why not?

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Number Talk – Defining Features

The chart below outlines some of the core features of a Number Talk that distinguish it from any other mathematical discussion about a problem.

Facilitation Feature	Student Experience
Problems are written and read publicly, but students solve mentally (no pencil and paper or white boards)	 Students develop efficiency, accuracy and fluency with mathematical thinking using mental math. Students move away from a reliance on standard algorithms and strict memorization, and move into sensemaking and sharing their reasoning around the mathematics.
Wait time	• All students have time to reflect upon and struggle with mental math and/or come up with multiple ways of solving
Silent signals as mode of response ("I have an answer" "I have 2 strategies") Silent validation of who got the same answer / who agrees or disagrees with an answer	 Students are not distracted by hands in the air, or by others who have found an answer quickly and want to share immediately. Students are motivated to come up with more than one way of solving. Emphasis is placed on the thinking process more than the answer itself. Students interact with each other, not just with the teacher
Surface all answers up front, including mistakes	 Mistakes are treated as learning opportunities Students agree with and/or critique the reasoning of others
Turn and Talk (optional)	 Every student has an opportunity to share her/his way of thinking about and solving the problem Students articulate ideas with a partner before engaging in large group academic discussion
Teacher begins scribing /representing student's strategy <i>after</i> student has finished explaining and without steering student in a particular direction. Teacher confirms with the presenter that his/her thinking is properly represented.	 Multiple strategies are made public Students see different ways to record a mental process Scribing reflects student's actual process, and not a specific, anticipated solution path Students feel ownership of their own strategies

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 Engagement /participation /comprehension questions after strategies are shared. Who did it exactly the same way as ? ("raise your hand if") Can you do that? Is that legal? Did everyone understand's way? Can someone explain's strategy in your own words? Who has another way of solving it? 	 Students make sense of each other's strategies Students see multiple ways of mentally solving problems, make connections between different ways of solving problems Students talk about their own and each other's thinking
--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------

Number Talk Planning Tools

The following pages include two different blank templates for planning a Number Talk as part of math lesson. The blank templates are followed by examples of completed templates for Number Talks.

The lesson planning templates are intended to guide a teacher's thinking as s/he prepares to facilitate a Number Talk, including anticipating student responses, considering possible ways to scribe different strategies, and identifying questions that will elicit student thinking and prompt students to make sense of each others' ideas. Thinking through each of these steps is important as teachers build familiarity with the strategy.

Anticipating student responses is a particularly crucial step in preparing to facilitate a Number Talk. Because they are developing both their understanding of the mathematics and their ability to articulate their thinking, students will often share strategies that are difficult to understand, either because the reasoning is complicated or because their language is not precise, or both. This can be particularly true for younger students. Anticipating student responses before presenting t problem to the class, and giving thought to the kinds of strategies students might apply to the problem, helps to ensure that the teacher will be able to find the mathematical logic in any student's contribution. Asking questions that encourage students to elaborate, or having other students paraphrase, can also help to reveal more of a student's intention and support the student in articulating his/her thoughts.

Once Number Talks become a routine part of classroom practice with a group of students, the procedures for how students signal that they have an answer in mind, how the Number Talk is framed, and how answers are shared before strategies are discussed may become habits for both teacher and students and will require less formal planning. At that point, teacher planning can focus more narrowly on anticipating responses and identifying connections a teacher hopes students will recognize or specific strategies that a teacher hopes will surface through the discussion.

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Number Talk Lesson Planning Template 1: Narrative

Grade Level:

Unit:

Core Math Idea: Number

Talk Problem:

Anticipated student methods and how to represent them:

During the Lesson

Frame for the activity: We are using a Number Talk to share different strategies for how we mentally approach a problem. Each person's role is to work on explaining their own thinking clearly, and to listen to other's explanations as well.

Maximum length of quiet time:

Silent signal when students are ready:

Process for sharing out:

- •
- •

Questions to orchestrate the class conversation about strategies:

Wrapping Up:

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Number Talk Lesson Plan 1: Elementary Sample

Grade Level: 3-5 Unit: Multiplication and Division

Core Math Idea: Students may be hindered in this unit because they are not yet fluent with basic addition and subtraction facts. So in this Number Talk, I will focus on adding and subtracting single and double digit numbers mentally, and specifically on the idea of doubles plus / minus one.

Number Talk Problem(s): 15 + 16 (FIRST IN A SERIES, TO BE FOLLOWED BY 15 + 14; 20 + 21; 22 + 23; 22 + 21)

Anticipated student methods and how to represent them:

Standard algorithm (stack them in your head)	15 <u>+16</u>
Count on fingers:	15, 16, 17, 31 (use open number line to represent single jumps)
Add 10 then add six	15 + 10 = 25 25 + 6 = 31
Double 15, then add one more:	15 + 15 = 30 30 + 1 = 31
Add 1O and 1O, then add 5, then add 6	10 + 10 = 20 20 + 5 = 25 25 + 6 = 31

During the Lesson

Frame for the activity: We are using a Number Talk to share different strategies for how we mentally approach a problem. Each person should be ready to explain their process, and to listen to understand someone else's.

Maximum length of quiet time: 2 min

Silent signal when students are ready: Thumb up in front of your chest when you have an answer. Raise another finger for each different strategy you think of.

Process for sharing out:

- Talk to your partner about your strategy.
- Volunteers, what number did you get for your solution? (Record all responses)
- After sharing, poll the class raise hand if you got this value

Questions to orchestrate the class conversation about strategies

- Who would like to share how they got their answer?
- I heard you say _____, did I hear correctly?
- Did anyone use a different method?
- Can someone explain _____'s strategy in their own words?
- Please raise your hand if you understand what _____ just shared.

Wrapping Up: Questions I might ask:

• Can you find two strategies that are similar? How are they the same?

Look at all of these strategies. Which new strategy would you want to try to use tomorrow? MATHEMATICS • GRADE 2• Grade Level Overview Georgia Department of Education Dr. John D. Barge, State School Superintendent July 2014 • Page 43 of 58 All Rights Reserved

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Number Talk Lesson Planning Template 2:Chart

Grade Level: Core Math Idea:

Unit:

Number Talk Problem	Possible Strategies & Method of Recording	Questions to Students
Follow up Problems (series)		Wrap Up
Academic Language	-	

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Number Talk Lesson Plan 2: Elementary Sample

Grade Level: 3-5

Unit: Multiplication and Division

Core Math Idea: Adding and subtracting single and double digit numbers mentally, and specifically the idea of doubles plus/minus one.

Number Talk Problem	Possible Strategies & Method of Recording	Questions to Students	
15 + 16	Standard algorithm (stack in your head): 15 ± 16 Count on fingers: 15, 16, 17, 31 (use open number line to represent single jumps) Add 10 then add six: 15 + 10 = 25	 Who would like to share how they got their answer? I heard you say, did I hear correctly? Did anyone use a different method? Can someone explain's strategy in their own words? Please raise your hand if you understand what just shared. Wrap Up 	
Follow up Problems (series)	25 +5 = 31		
15+14 20+21 22+23	Double 15, then add one more: 15 + 15 = 30 30 + 1 = 31	Can you find two strategies that are similar? How are they the same?	
22 + 21	Add 10 and 10, then add 5, then add 6 10+10=20 20+5=25	Look at all of these strategies. Which strategy would you want to try to use	
Academic Language	25 + 6 = 31	tomorrow?	
addend, sum, total, doubles, doubles plus one, doubles minus one			

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Estimation 180

Estimation is a skill that has many applications, such as checking computation answers quickly. Engaging in regular estimation activities will develop students' reasoning skills, number sense, and increase their repertoire of flexible and efficient strategies. As students gain more experiences with estimation, their accuracy will improve.

According to John Van de Walle, there are three types of estimation that students should practice:

- Measurement estimation determining an approximate measurement, such as weight, length, or capacity
- Quantity estimation approximating the number of items in a collection
- Computational estimation determining a number that is an approximation of a computation

One resource which provides contexts for all three types of estimation is Andrew Stadel's website, <u>http://www.estimation180.com/</u>. In his website, Mr. Stadel has posted daily estimation contexts. Here are his directions for using his website:

- 1. Click on a picture.
- 2. Read the question.
- 3. Look for context clues.
- 4. Make an estimate.
- 5. Tell us how confident you are.
- 6. Share your reasoning (what context clues did you use?).
- 7. See the answer.
- 8. See the estimates of others.

The most important part is step #6. After you make an estimate, feel free to give a brief description. It's so valuable to a classroom when students share their logic or use of context clues when formulating an estimate.

Andrew Stadel has collaborated with Michael Fenton to create a recording sheet for students to use with the estimation contexts on the website. The recording sheet can also be found at http://www.estimation180.com/. Here are his directions for the recording sheet:

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Day #	Description	↓ Too Low	Too High †	My Estimate	My Reasoning	Answer	Error	Error as %
Ex. A	Tyler's age (months)	24	36	30	He looks a little older than my cousin (who is 2)	26	⊕ 4 -	4/26 ≈ 15%
Ex. B	Bohemian Rhapsody	4:00	5:00	4:30	10% of song = 30 sec 300 sec total = 5 min	5:56	+ 86	86/356 ≈ 24%
							+	

Column use descriptions from Andrew Stadel:

Day

In Estimation 180's first year, I was just trying to keep up with creating these estimation challenges in time for use in my own classroom. There really wasn't a scope and sequence involved. That said, now that there are over 160 estimation challenges available, teachers and students can use them at any time throughout the school year and without completing them in sequential order. Therefore, use the *Day* # column simply to number your daily challenges according to the site. Tell your students or write it up on the board that you're doing the challenge from <u>Day 135</u> even though you might be on the fifth day of school.

Description

In my opinion, this column is more important than the *Day* # column. Don't go crazy here. Keep it short and sweet, but as specific as possible. For example, there's a lot of scattered height estimates on the site. Don't write down "How tall?" for <u>Day 110</u>. Instead write "Bus height" because when you get to <u>Day 111</u>, I'd write in "Parking structure height". I believe the teacher has the ultimate say here, but it can be fun to poll your students for a short description in which you all can agree. Give students some ownership, right? If unit measurement is involved, try and sneak it in here. Take Day 125 for instance. I'd suggest entering "Net Wt. (oz.) of lg Hershey's bar." Keep in mind that Day 126 asks the same question, but I'd suggest you encourage your class to use pounds if they don't think of it.

*By the way, sometimes unit measurement(s) are already included in the question. Use discretion.

Too Low

Think of an estimate that is too low.

Don't accept one (1), that's just rubbish, unless one (1) is actually applicable to the context of the challenge. Stretch your students. Think of it more as an answer that's too low, but reasonably close. After all, this is a site of estimation challenges, not gimmes.

Too High

Refer to my notes in *Too Low*. Just don't accept 1 billion unless it's actually applicable. Discuss with students the importance of the *Too Low* and *Too High* sections: we are trying to eliminate wrong answers while creating a range of possible answers.

My Estimate

This is the place for students to fill in their answer. If the answer requires a unit of measurement, we better see one. Not every estimation challenge is "How many..." marshmallows? or christmas

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lights? or cheese balls?

Even if a unit of measurement has already been established (see the *Description* notes), I'd still encourage your students to accompany their numerical estimate with a unit of measurement.



For example, on Day 41, "What's the height of the Giant [Ferris] Wheel?" use what makes sense to you, your students and your country's customary unit of measurement. Discuss the importance of unit measurements with students. Don't accept 108. What does that 108 represent? Pancakes? Oil spills? Bird droppings? NO! It represents 108 feet.

My Reasoning

The *My Reasoning* section is the most recent addition to the handout and I'm extremely thrilled about it. This is a student's chance to shine! Encourage their reasoning to be short and sweet. When a student writes something down, they'll be more inclined to share it or remember it. Accept bullet points or phrases due to the limited space. We don't need students to write paragraphs. However, we are looking for students to identify any context clues they used, personal experiences, and/or prior knowledge. Hold students accountable for their reasoning behind the estimate of the day.

Don't let student reasoning go untapped! If you're doing a sequence of themed estimation challenges, don't accept, "I just guessed" after the first day in the sequence. For example, if you're doing the flight distance themed estimate challenges starting on Day 136, you will establish the distance across the USA on the first day. Sure, go ahead and guess on Day 136, but make sure you hold students accountable for their reasoning every day thereafter.

Have students share their reasoning before and after revealing the answer. Utilize Think-Pair-Share. This will help create some fun conversations *before* revealing the answer. After revealing the answer, get those who were extremely close (or correct) to share their reasoning. I bet you'll have some great mathematical discussions. I'm also curious to hear from those that are way off and how their reasoning could possibly be improved.

I'd say the *My Reasoning* section was born for Mathematical Practice 3: *Construct viable arguments and critique the reasoning of others*. Keep some of these thoughts in mind regarding Mathematical Practice 3:

- Explain and defend your estimate.
- Construct a detailed explanation referencing context clues, prior knowledge, or previous experiences.
- Invest some confidence in it.
- Try to initiate a playful and respectful argument in class.
- Ask "Was anyone convinced by this explanation? Why? Why not?" or "Are you guys going to let [student name] off the hook with that explanation?"

There's reasoning behind every estimate (not guess).

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- Find out what that reasoning is!
- DON'T let student reasoning go untapped!

Answer

Jot down the revealed answer. I'd also encourage students to write down the unit of measurement used in the answer. The answer might use a different unit of measurement than what you and your class agreed upon. Take the necessary time to discuss the most relative unit of measurement. I might be subjectively wrong on some of the answers posted. As for more thoughts on unit of measurement, refer to the *My Estimate* notes above. Continue having mathematical discussion after revealing the answer. Refer to my notes regarding the use of Mathematical Practice 3 in the *My Reasoning* section.

Error

Find the difference between *My Estimate* and *Answer*. Have students circle either the "+" or the "-" if they didn't get it exactly correct.

- + Your estimate was greater than (above) the actual answer.
- Your estimate was less than (below) the actual answer.

Mathematize the World through Daily Routines

The importance of continuing the established classroom routines cannot be overstated. Daily routines must include such obvious activities such as taking attendance, doing a lunch count, determining how many items are needed for snack, lining up in a variety of ways (by height, age, type of shoe, hair color, eye color, etc.), daily questions, 99 chart questions, and calendar activities. They should also include less obvious routines, such as how to select materials, how to use materials in a productive manner, how to put materials away, how to open and close a door, how to do just about everything! An additional routine is to allow plenty of time for children to explore new materials before attempting any directed activity with these new materials. The regular use of the routines are important to the development of students' number sense, flexibility, and fluency, which will support students' performances on the tasks in this unit.

Workstations and Learning Centers

It is recommended that workstations be implemented to create a safe and supportive environment for problem solving in a standards based classroom. These workstations typically occur during the "exploring" part of the lesson, which follows the mini-lesson. Your role is to introduce the concept and allow students to identify the problem. Once students understand what to do and you see that groups are working towards a solution, offer assistance to the next group.

Groups should consist of 2-5 students and each student should have the opportunity to work with all of their classmates throughout the year. Avoid grouping students by ability. Students in the lower group will not experience the thinking and language of the top group, and top students will not hear the often unconventional but interesting approaches to tasks in the lower group (28, Van de Walle and Lovin 2006).

In order for students to work efficiently and to maximize participation, several guidelines must be in place (Burns 2007):

1. You are responsible for your own work and behavior.

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- 2. You must be willing to help any group member who asks.
- 3. You may ask the teacher for help only when everyone in your group has the same question.

These rules should be explained and discussed with the class so that each student is aware of the expectations you have for them as a group member. Once these guidelines are established, you should be able to successfully lead small groups, which will allow you the opportunity to engage with students on a more personal level while providing students the chance to gain confidence as they share their ideas with others.

The types of activities students engage in within the small groups will not always be the same. Facilitate a variety of tasks that will lead students to develop proficiency with numerous concepts and skills. Possible activities include: math games, related previous Framework tasks, problems, and computer-based activities. With all tasks, regardless if they are problems, games, etc. include a recording sheet for accountability. This recording sheet will serve as a means of providing you information of how a child arrived at a solution or the level at which they can explain their thinking (Van de Walle 2006).

Games

"A game or other repeatable activity may not look like a problem, but it can nonetheless be problem based. The determining factor is this: Does the activity cause students to be reflective about new or developing relationships? If the activity merely has students repeating procedure without wrestling with an emerging idea, then it is not a problem-based experience. However the few examples just mentioned and many others do have children thinking through ideas that are not easily developed in one or two lessons. In this sense, they fit the definition of a problembased task.

Just as with any task, some form of recording or writing should be included with stations whenever possible. Students solving a problem on a computer can write up what they did and explain what they learned. Students playing a game can keep records and then tell about how they played the game- what thinking or strategies they used." (Van de Walle and Lovin, Teaching Student-Centered Mathematics: K-3, page 26)

Journaling

"Students should be writing and talking about math topics every day. Putting thoughts into words helps to clarify and solidify thinking. By sharing their mathematical understandings in written and oral form with their classmates, teachers, and parents, students develop confidence in themselves as mathematical learners; this practice also enables teachers to better monitor student progress." NJ DOE

"Language, whether used to express ideas or to receive them, is a very powerful tool and should be used to foster the learning of mathematics. Communicating about mathematical ideas is a way for students to articulate, clarify, organize, and consolidate their thinking. Students, like adults, exchange thoughts and ideas in many ways—orally; with gestures; and with pictures, objects,

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and symbols. By listening carefully to others, students can become aware of alternative perspectives and strategies. By writing and talking with others, they learn to use more-precise mathematical language and, gradually, conventional symbols to express their mathematical ideas. Communication makes mathematical thinking observable and therefore facilitates further development of that thought. It encourages students to reflect on their own knowledge and their own ways of solving problems. Throughout the early years, students should have daily opportunities to talk and write about mathematics." NCTM

When beginning math journals, the teacher should model the process initially, showing students how to find the front of the journal, the top and bottom of the composition book, how to open to the next page in sequence (special bookmarks or ribbons), and how to date the page. Discuss the usefulness of the book, and the way in which it will help students retrieve their math thinking whenever they need it.

When beginning a task, you can ask, "What do we need to find out?" and then, "How do we figure it out?" Then figure it out, usually by drawing representations, and eventually adding words, numbers, and symbols. During the closing of a task, have students show their journals with a document camera or overhead when they share their thinking. This is an excellent opportunity to discuss different ways to organize thinking and clarity of explanations.

Use a composition notebook (the ones with graph paper are terrific for math) for recording or drawing answers to problems. The journal entries can be from Frameworks tasks, but should also include all mathematical thinking. Journal entries should be simple to begin with and become more detailed as the children's problem-solving skills improve. Children should always be allowed to discuss their representations with classmates if they desire feedback. The children's journal entries demonstrate their thinking processes. Each entry could first be shared with a "buddy" to encourage discussion and explanation; then one or two children could share their entries with the entire class. Don't forget to praise children for their thinking skills and their journal entries! These journals are perfect for assessment and for parent conferencing. The student's thinking is made visible!

GENERAL QUESTIONS FOR TEACHER USE

Adapted from Growing Success and materials from Math GAINS and TIPS4RM

Reasoning and Proving

- How can we show that this is true for all cases?
- In what cases might our conclusion not hold true?
- How can we verify this answer?
- Explain the reasoning behind your prediction.
- Why does this work?
- What do you think will happen if this pattern continues?
- Show how you know that this statement is true.
- Give an example of when this statement is false.
- Explain why you do not accept the argument as proof.
- How could we check that solution?

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Reflecting

- Have you thought about...?
- What do you notice about...?
- What patterns do you see?
- Does this problem/answer make sense to you?
- How does this compare to...?
- What could you start with to help you explore the possibilities?
- How can you verify this answer?
- What evidence of your thinking can you share?
- Is this a reasonable answer, given that...?
- How can you change . . .

Selecting Tools and Computational Strategies

- How did the learning tool you chose contribute to your understanding/solving of the problem? assist in your communication?
- In what ways would [name a tool] assist in your investigation/solving of this problem?
- What other tools did you consider using? Explain why you chose not to use them.
- Think of a different way to do the calculation that may be more efficient.
- What estimation strategy did you use?

Connections

- What other math have you studied that has some of the same principles, properties, or procedures as this?
- How do these different representations connect to one another?
- When could this mathematical concept or procedure be used in daily life?
- What connection do you see between a problem you did previously and today's problem?

Representing

- What would other representations of this problem demonstrate?
- Explain why you chose this representation.
- How could you represent this idea algebraically? graphically?
- Does this graphical representation of the data bias the viewer? Explain.
- What properties would you have to use to construct a dynamic representation of this situation?
- In what way would a scale model help you solve this problem?
- Show me an example of . . .

QUESTIONS FOR TEACHER REFLECTION

- How did I assess for student understanding?
- How did my students engage in the 8 mathematical practices today?

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- How effective was I in creating an environment where meaningful learning could take place?
- How effective was my questioning today? Did I question too little or say too much?
- Were manipulatives made accessible for students to work through the task?
- Name at least one positive thing about today's lesson and one thing you will change.
- How will today's learning impact tomorrow's instruction?

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MATHEMATICS DEPTH-OF-KNOWLEDGE LEVELS

Level 1 (Recall) includes the recall of information such as a fact, definition, term, or a simple procedure, as well as performing a simple algorithm or applying a formula. That is, in mathematics a one-step, well-defined, and straight algorithmic procedure should be included at this lowest level. Other key words that signify a Level 1 include "identify," "recall," "recognize," "use," and "measure." Verbs such as "describe" and "explain" could be classified at different levels depending on what is to be described and explained.

Level 2 (Skill/Concept) includes the engagement of some mental processing beyond a habitual response. A Level 2 assessment item requires students to make some decisions as to how to approach the problem or activity, whereas Level 1 requires students to demonstrate a rote response, perform a well-known algorithm, follow a set procedure (like a recipe), or perform a clearly defined series of steps. Keywords that generally distinguish a Level 2 item include "classify," "organize," "estimate," "make observations," "collect and display data," and "compare data." These actions imply more than one step. For example, to compare data requires first identifying characteristics of the objects or phenomenon and then grouping or ordering the objects. Some action verbs, such as "explain," "describe," or "interpret" could be classified at different levels depending on the object of the action. For example, if an item required students to explain how light affects mass by indicating there is a relationship between light and heat, this is considered a Level 2. Interpreting information from a simple graph, requiring reading information from the graph, also is a Level 2. Interpreting information from a complex graph that requires some decisions on what features of the graph need to be considered and how information from the graph can be aggregated is a Level 3. Caution is warranted in interpreting Level 2 as only skills because some reviewers will interpret skills very narrowly, as primarily numerical skills, and such interpretation excludes from this level other skills such as visualization skills and probability skills, which may be more complex simply because they are less common. Other Level 2 activities include explaining the purpose and use of experimental procedures; carrying out experimental procedures; making observations and collecting data; classifying, organizing, and comparing data; and organizing and displaying data in tables, graphs, and charts.

Level 3 (Strategic Thinking) requires reasoning, planning, using evidence, and a higher level of thinking than the previous two levels. In most instances, requiring students to explain their thinking is a Level 3. Activities that require students to make conjectures are also at this level. The cognitive demands at Level 3 are complex and abstract. The complexity does not result from the fact that there are multiple answers, a possibility for both Levels 1 and 2, but because the task requires more demanding reasoning. An activity, however, that has more than one possible answer and requires students to justify the response they give would most likely be a Level 3. Other Level 3 activities include drawing conclusions from observations; citing evidence and developing a logical argument for concepts; explaining phenomena in terms of concepts; and using concepts to solve problems.

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DOK cont'd...

Level 4 (Extended Thinking) requires complex reasoning, planning, developing, and thinking most likely over an extended period of time. The extended time period is not a distinguishing factor if the required work is only repetitive and does not require applying significant conceptual understanding and higher-order thinking. For example, if a student has to take the water temperature from a river each day for a month and then construct a graph, this would be classified as a Level 2. However, if the student is to conduct a river study that requires taking into consideration a number of variables, this would be a Level 4. At Level 4, the cognitive demands of the task should be high and the work should be very complex. Students should be required to make several connections—relate ideas *within* the content area or *among* content areas—and have to select one approach among many alternatives on how the situation should be solved, in order to be at this highest level. Level 4 activities include designing and conducting experiments; making connections between a finding and related concepts and phenomena; combining and synthesizing ideas into new concepts; and critiquing experimental designs.

DEPTH AND RIGOR STATEMENT

By changing the way we teach, we are not asking children to learn less, we are asking them to learn more. We are asking them to mathematize, to think like mathematicians, to look at numbers before they calculate, to think rather than to perform rote procedures. Children can and do construct their own strategies, and when they are allowed to make sense of calculations in their own ways, they understand better. In the words of Blaise Pascal, "We are usually convinced more easily by reasons we have found ourselves than by those which have occurred to others."

By changing the way we teach, we are asking teachers to think mathematically, too. We are asking them to develop their own mental math strategies in order to develop them in their students. Catherine Twomey Fosnot and Maarten Dolk, *Young Mathematicians at Work*.

While you may be tempted to explain and show students how to do a task, much of the learning comes as a result of making sense of the task at hand. Allow for the productive struggle, the grappling with the unfamiliar, the contentious discourse, for on the other side of frustration lies understanding and the confidence that comes from "doing it myself!"

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Problem	Solving	Rubric ((K-2)

SMP	1-Emergent	2-Progressing	3- Meets/Proficient	4-Exceeds
Make sense of problems and persevere in solving them.	The student was unable to explain the problem and showed minimal perseverance when identifying the purpose of the problem.	The student explained the problem and showed some perseverance in identifying the purpose of the problem, and selected and applied an appropriate problem solving strategy that lead to a partially complete and/or partially	The student explained the problem and showed perseverance when identifying the purpose of the problem, and selected an applied and appropriate problem solving strategy that lead to a generally complete and accurate solution.	The student explained the problem and showed perseverance by identifying the purpose of the problem and selected and applied an appropriate problem solving strategy that lead to a thorough and accurate solution.
Attends to precision	The student was unclear in their thinking and was unable to communicate mathematically.	accurate solution. The student was precise by clearly describing their actions and strategies, while showing understanding and using appropriate vocabulary in their process of finding solutions.	The student was precise by clearly describing their actions and strategies, while showing understanding and using grade-level appropriate vocabulary in their process of finding solutions.	The student was precise by clearly describing their actions and strategies, while showing understanding and using above-grade-level appropriate vocabulary in their process of finding solutions.
Reasoning and explaining	The student was unable to express or justify their opinion quantitatively or abstractly using numbers, pictures, charts or words.	The student expressed or justified their opinion either quantitatively OR abstractly using numbers, pictures, charts OR words.	The student expressed and justified their opinion both quantitatively and abstractly using numbers, pictures, charts and/or words.	The student expressed and justified their opinion both quantitatively and abstractly using a variety of numbers, pictures, charts and words.
Models and use of tools	The student was unable to select an appropriate tool, draw a representation to reason or justify their thinking.	The student selected an appropriate tools or drew a correct representation of the tools used to reason and justify their response.	The student selected an efficient tool and/or drew a correct representation of the efficient tool used to reason and justify their response.	The student selected multiple efficient tools and correctly represented the tools to reason and justify their response. In addition this students was able to explain why their tool/ model was efficient
Seeing structure and generalizing	The student was unable to identify patterns, structures or connect to other areas of mathematics and/or real-life.	The student identified a pattern or structure in the number system and noticed connections to other areas of mathematics or real- life.	The student identified patterns or structures in the number system and noticed connections to other areas of mathematics and real- life.	The student identified various patterns and structures in the number system and noticed connections to multiple areas of mathematics and real-life.

Creation of Richmond County Schools

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SUGGESTED LITERATURE

- A Place for Zero by Angeline LoPresti
- A Remainder of One by Elinor J. Pinczes
- Bunny Money by Rosemary Wells
- Captain Invincible and the Space Shapes by Stuart J. Murphy
- Each Orange has 8 slices: A Counting Book by P. Giganti
- Gator Pie by Louise Mathews
- *How Big Is a Foot?* by Rolf Myller
- Inch by Inch by Leo Lionni
- It's About Time! By Stuart J. Murphy
- Jim and the Beanstalk by Raymond Briggs
- Lemonade for Sale by Stuart Murphy
- *Math Appeal* by Greg Tang
- *Measuring Penny* by Loreen Leedy
- *Mouse Count* by Ellen Stoll Walsh
- *Ready, Set, Hop* by Stuart Murphy
- The Greedy Triangle by Marilyn Burns
- The Grouchy Lady Bug by Eric Carle
- *The Shape of Things* by Dayle Ann Dodds
- *Twelve Snails to One Lizard* by Susan Highower
- What Comes in 2's, 3's, and 4's? by Suzanne Aker
- When a Line Bends, a Shape Begins by Rhonda G. Greene

TECHNOLOGY LINKS

- <u>http://www.gpb.org/education/common-core</u>
- <u>http://catalog.mathlearningcenter.org/apps</u>
- http://nzmaths.co.nz/digital-learning-objects
- <u>http://www.fi.uu.nl/toepassingen/00203/toepassing_rekenweb.xml?style=rekenweb&lang</u> <u>uage=en&use=game</u>
- https://www.georgiastandards.org/resources/Pages/Tools/LearningVillage.aspx
- <u>https://www.georgiastandards.org/Common-Core/Pages/Math.aspx</u>
- <u>https://www.georgiastandards.org/Common-Core/Pages/Math-PL-Sessions.aspx</u>

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RESOURCES CONSULTED

Content:

Ohio DOE http://www.ode.state.oh.us/GD/Templates/Pages/ODE/ODEPrimary.aspx?page=2&TopicRelatio nID=1704 Arizona DOE http://www.azed.gov/standards-practices/mathematics-standards/ Nzmaths http://nzmaths.co.nz/

Teacher/Student Sense-making:

http://www.youtube.com/user/mitcccnyorg?feature=watch http://www.insidemathematics.org/index.php/video-tours-of-inside-mathematics/classroomteachers/157-teachers-reflect-mathematics-teaching-practices https://www.georgiastandards.org/Common-Core/Pages/Math.aspx or http://secc.sedl.org/common_core_videos/

Journaling:

http://www.kindergartenkindergarten.com/2010/07/setting-up-math-problemsolvingnotebooks.html

Community of Learners:

http://www.edutopia.org/math-social-activity-cooperative-learning-video http://www.edutopia.org/math-social-activity-sel http://www.youtube.com/user/responsiveclassroom/videos http://www.responsiveclassroom.org/category/category/first-weeks-school

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